

# Solving Minimum Cost Lifted Multicut Problems by Node Agglomeration



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## Lifted Multicut Problem

Solutions to the Minimum Cost Lifted Multicut Problems (**MCLMP**)s correspond to decomposition of a graph into an optimal number of segments.

Properties of MCLMP:

- NP-hard problem
- No need to specify the number of segments
- Generalization of MCMPs (correlation clustering)
- Consider long range connections

## Related Work

GAEC [1] properties:

- Guaranteed worst case complexity
- Low quality results
- Short run-time

KLj [1] and FM-R [2] properties:

- Without guaranteed worst case complexity
- High quality results
- Long run-time

Exemplary results of KLj and GAEC with lifting radius 10



KLj

GAEC

## Contributions

We propose 2 variants of a heuristic solver based on GAEC [1]:

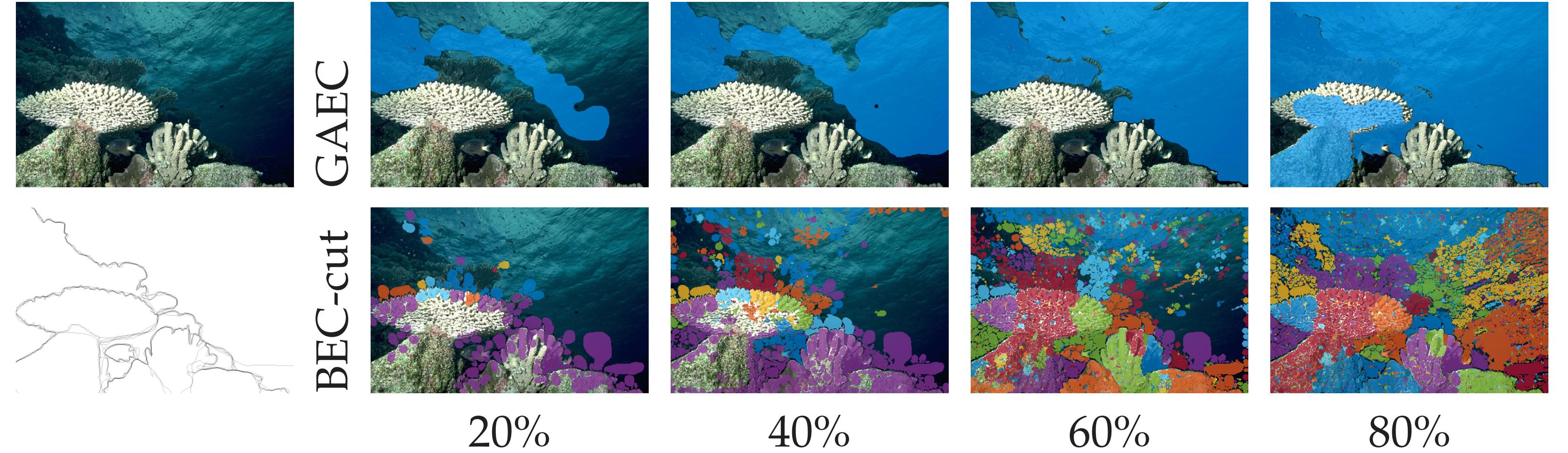
1. Balanced Edge Contraction (**BEC**)
2. **BEC-cut**

Properties of the proposed solvers:

- Generated solutions have qualities close to KLj [1]
- Computation time is similar to GAEC [1]
- Guaranteed worst case complexity

## Problem Specification

Visualization of intermediate states during execution of GAEC [1] and the proposed **BEC-cut** solver



## Technical Details

### Balanced Edge Contraction (BEC)

Creates balanced clusters

*Criteria:*

Assuming separate clusters  $a'$  and  $b'$  and their merging cost  $\chi_{a'b'}$  on graph  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$

$$ab := \operatorname{argmax}_{a'b' \in \mathcal{E}} \frac{\chi_{a'b'}}{|a'| + |b'|}$$

### BEC-cut

Creates clusters along the object boundaries

*Criteria:*

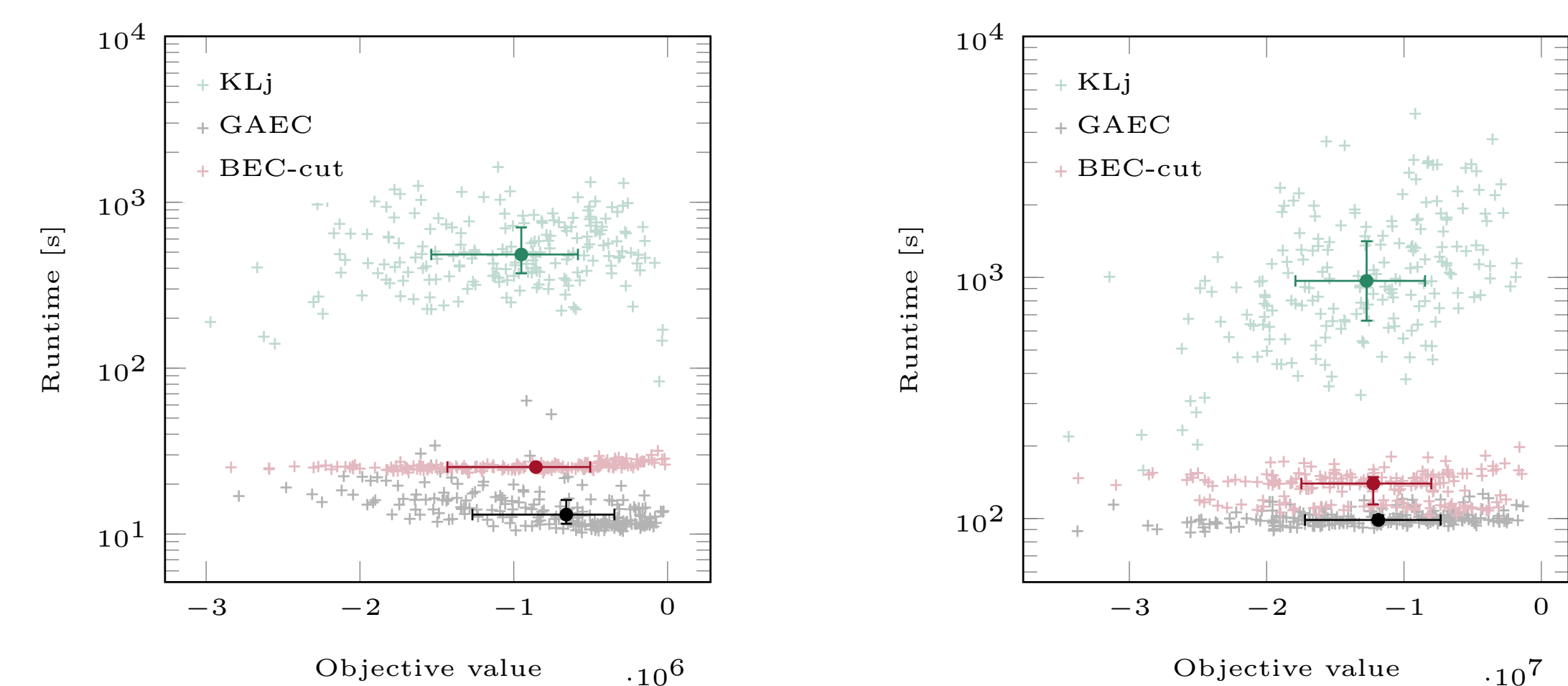
Assuming separate clusters  $a'$  and  $b'$  and outgoing costs  $\zeta_{a'}$  and  $\zeta_{b'}$

$$\begin{aligned} \mathcal{S} &:= \operatorname{argmax}_{a'b' \in \mathcal{E}} \frac{\chi_{a'b'}}{|a'| + |b'|} \\ ab &:= \operatorname{argmin}_{a'b' \in \mathcal{S}} \frac{\zeta_{a'} + \zeta_{b'} - 2\chi_{a'b'}}{|a'| + |b'|} \end{aligned}$$

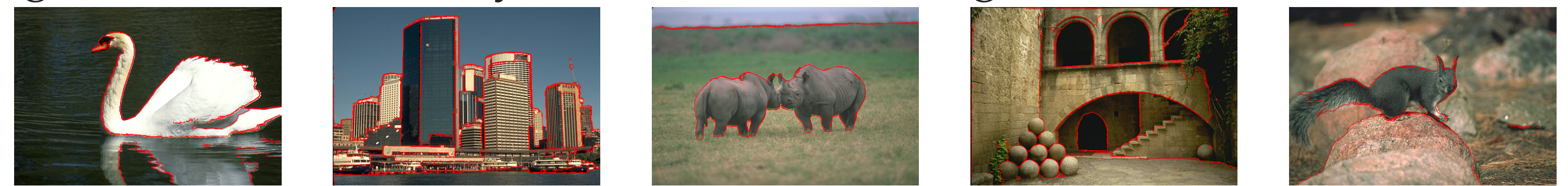
Priority queue is used for an ordered sequence of costs.

## Image Decomposition

Comparison of **BEC**, **BEC-cut**, GAEC [1] and KLj [1] on BSDS500 with lifting radius 10 (left) and 20 (right)



Exemplary segmentation results by **BEC-cut** with lifting radius 10

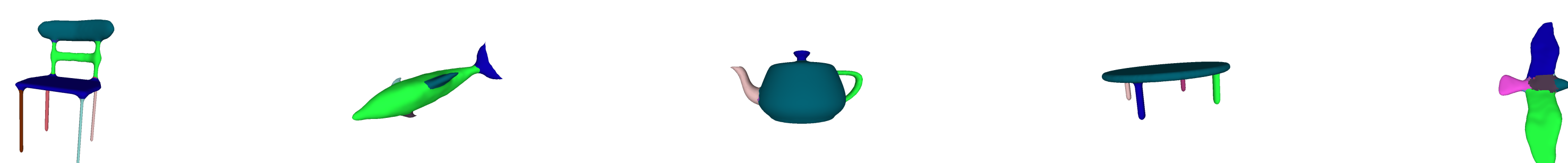


## Mesh Segmentation

Average computation time and objective value of the different solvers

	GAEC [1]	KLj-GAEC [1]	BEC	BEC-cut
Avg. Comp. time [s]	576	755	589	574
Avg. Objective Value	-17840450	-18988930	-18484140	-18057480

Exemplary segmentation results by **BEC-cut**



## References

- [1] M. Keuper, E. Levinkov, N. Bonneel, G. Lavoué, T. Brox and B. Andres. Efficient Decomposition of Image and Mesh Graphs by Lifted Multicuts In ICCV '15
- [2] T. Beier, B. Andres, U. Köthe and F. A. Hamprecht. An Efficient Fusion Move Algorithm for the Minimum Cost Lifted Multicut Problem. In ECCV '16

## Future Direction

Providing good quality segmentation results in affordable amount of time motivates applying these solvers to the larger scale problems such as video segmentation.

## Paper Website

The paper and code for generating lifted multicut problems are available at

<http://web.informatik.uni-mannheim.de/akardoos/>

